The Twomey Effect
Twomey effect

• The paper(s) that “started it all”
  – Precursor papers
    • Physical basis for growth of cloud droplets dates back to equations for diffusional growth from Maxwell (1800s). Applied to cloud droplet growth by Kraus and Smith (1949), Howell (1949), Squires (1952).
    • Influence of composition of aerosol particles by Köhler (1921)
    • Twomey’s own prior work (e.g. Twomey 1959, Twomey and Warner 1967) provided a clear influence of the concentration of aerosol particles on the concentration of cloud droplets
    • Theoretical basis covered in ATMS 535
Comparison of Measurements of Cloud Droplets and Cloud Nuclei

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(Manuscript received 30 June 1967)

ABSTRACT

Samplings of cloud droplets were compared with airborne cloud nuclei measurements in air below cloud base. The number concentration of the cloud droplets agreed closely with the number obtained from the nuclei measurements.

Fig. 1. Comparison of mean droplet concentration observed in cloud with the concentration computed from the observed spectra of cloud nuclei for an updraft of 3 m sec\(^{-1}\). The dashed line represents exact agreement between observed and computed values.

Twomey effect

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  **POLLUTION AND THE PLANETARY ALBEDO**

  **S. TWOMEY**

  Institute of Atmospheric Physics, The University of Arizona, Tucson, Arizona 85721, U.S.A.

  *(First received 27 February 1974 and in final form 17 May 1974)*

**Abstract**—Addition of cloud nuclei by pollution can lead to an increase in the solar radiation reflected by clouds. The reflection of solar energy by clouds already may have been increased by the addition of man-made cloud nuclei. The albedo of a cloud is proportional to optical thickness for thin clouds, but changes more slowly with increasing thickness. The optical thickness is increased when the number of cloud nuclei is increased. Although the changes are small, the long-term effect on climate can be profound.

Twomey effect

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Twomey effect
a.k.a. the *first aerosol indirect effect*
A little math

- In the geometric limit where the drop size is larger than the wavelength of light \((r>\lambda)\), scattering of light is proportional to the total droplet surface area per volume \([Q_{ext}=2\) in Twomey’s Eqn. (1)]

- In the visible (where solar energy is most intense), \(\lambda=0.4-0.8\) micron, \(r\) for cloud drops typically 5-15 microns.

- Surface area of one drop: \(A_{drop} = 4\pi r^2\)

- Surface area of \(N\) drops per unit volume = \(4\pi Nr^2\)

- Optical thickness \(\tau = Q_{ext}\pi Nr^2 h = 2\pi Nr^2 h\) \[Twomey Eqn. 2\]

- Liquid water content \(L = (4/3)\pi\rho_w Nr^3\) [kg m\(^{-3}\)]

- Substitute for \(L\) into expression for optical thickness: \(\tau = \frac{3Lh}{2\rho_wr}\)

- Or, eliminating \(r\) and retaining \(N\), we can write \(\tau \propto N^{1/3} L^{2/3} h\)

- **Twomey’s key result**: For fixed liquid water content and cloud thickness, optical thickness increases with \(N^{1/3}\)
Relationship between solar reflectance and optical thickness

- Albedo increases with optical thickness, but is a concave function:
Beyond Twomey

Combine Twomey’s expression for optical thickness:

\[ \tau = kN^{1/3}L^{2/3}h \]

with simple expression for albedo, \( \alpha \approx \tau/(\tau + 7) \), to estimate the rate of change of albedo with \( N \) (termed the albedo susceptibility, Platnick and Twomey 1994), to obtain:

\[ \frac{d\alpha}{dN} = \frac{\alpha(1 - \alpha)}{3N} \]

This form, although not in the original Twomey (1974,77) papers, is the most instructive way to visualize the key results:

- Clouds with low \( N \) are most susceptible to an increase in \( N \)
- Clouds with albedos \( \sim 0.5 \) are more susceptible to increases in \( N \) than clouds with either lower or higher albedo.

Albedo susceptibility estimates from space

- MODIS instrument (multi-spectral radiometer) can estimate cloud optical thickness and effective radius to estimate $\frac{d\alpha}{dN}$

![Image](image.png)

Figure 4a. Monthly averages of absolute susceptibility ($\Delta N = 1 \text{ cm}^{-3}$, $w = 0.3 \text{ gm}^{-3}$) from MODIS Terra Level 3 $\tau$-$r_e$ joint histograms for January, April, July, and October 2005.