

# Probabilistic Weather Forecasting via Bayesian Model Averaging

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In collaboration with Cliff Mass, Susan Joslyn, and Jeff Baars  
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  - **⇒ the 4D probabilistic forecasting cube**

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  - **The model is:**

$$p(y|\tilde{y}_1, \dots, \tilde{y}_K) = \sum_{k=1}^K w_k N(a_k + b_k \tilde{y}_k, \sigma^2)$$

where  $w_k \geq 0$  and  $\sum_{k=1}^K w_k = 1$ .

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- The model is estimated from a training set of recent data at stations by maximum likelihood using the EM algorithm.
- Good results with a 25-day “moving window” training period.

# UW Ensemble Bayesian Model Averaging

## User's Guide

Param: Max 2m Temp (24-48 hrs)

Valid for 24 hours ending at:



Wed May 27, 2009 5 PM



[Jump to new date](#)

[Toggle Contour Lines OFF](#)

Plot Size:  Big  Medium  Small

Units:  Celsius  Fahrenheit

Grid Forecast:

Deterministic

Upper bound of interval

.9

Lower bound of interval

.1

Half-width of interval

Prob. param exceeds threshold

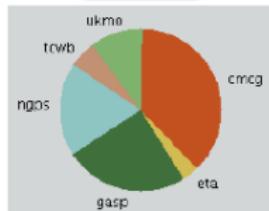
0

Greater than  Less than

Probability Distribution:

Latitude: 47.68049 Longitude: -122.2244

[Retrieve Data](#)



[BMA Weights](#)

Forecasts Error: **NORMAL: 2.16**

BMA Forecast Verification

Prob of freezing 0 Prob of precip > 1/4" Prob of precip > 1" Prob of high winds Prob of gale winds

degC

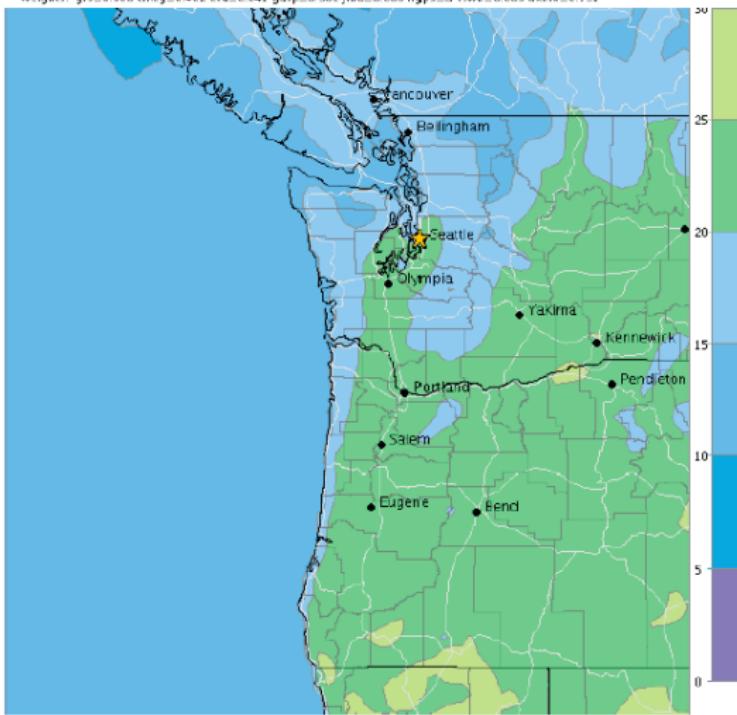
-23.0



46.0

BMA MAXT2 Forecast Init: 5/25/09 12:00 AM UTC (5/25/09 5:00 PM) Valid: 5/26/09 5:00 PM to 5/27/09 5:00 PM PT

Weights: gfs=0.300 cmcg=0.462 eta=0.641 gasp=0.302 jma=0.000 nsgs=0.000 trwb=0.063 ukmo=0.131



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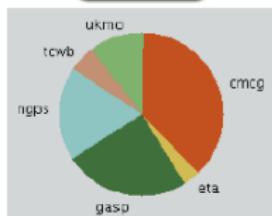
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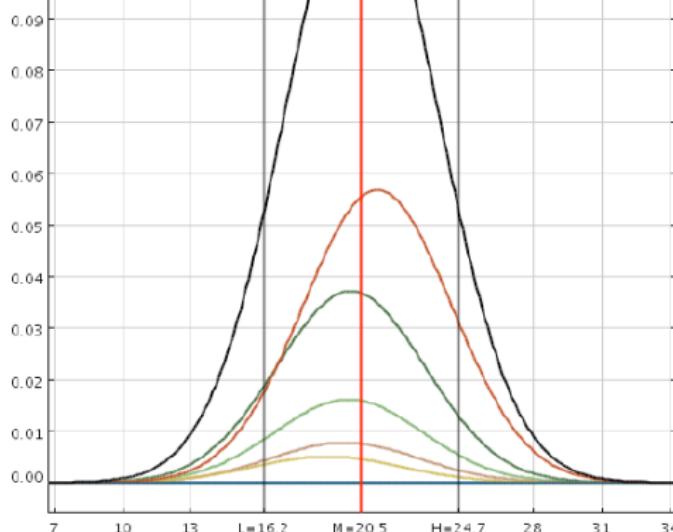
-23.0

H H H

16.2 20.5 24.7

48.0

Forecast PDF 0.0% MAXT2 < 0.0, Init: 5/26/2009 0Z Valid: 5/27/2009 0Z to 5/28/2009 0Z



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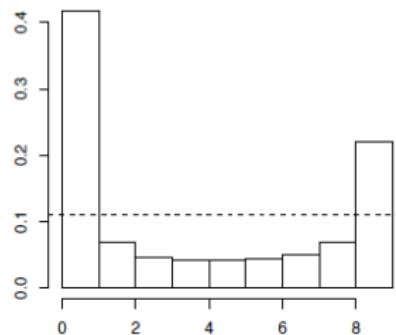
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Verification rank histogram  
for raw ensemble

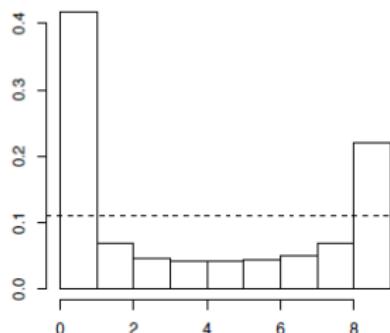


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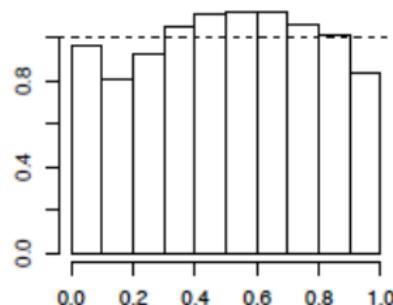
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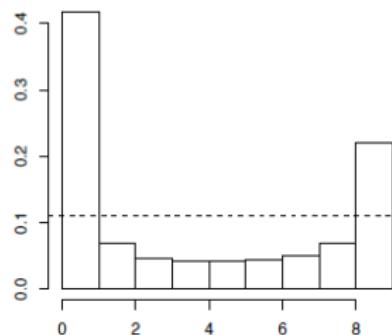


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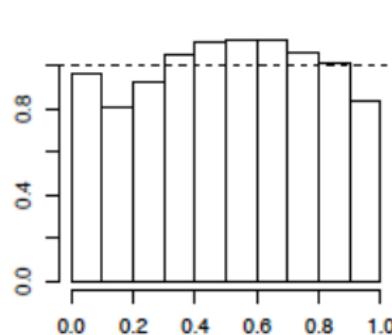
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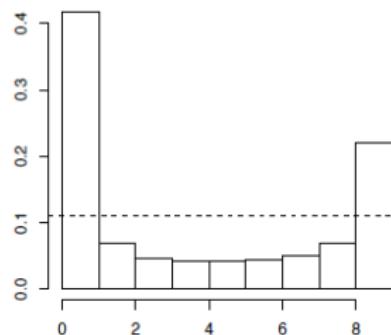
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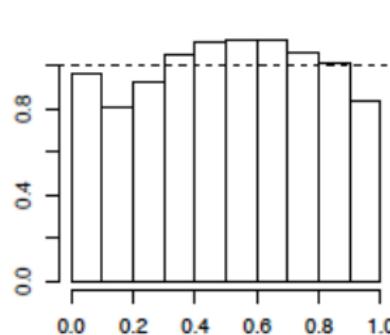
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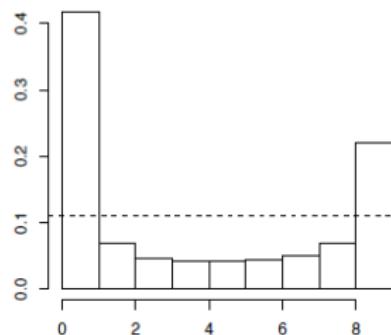
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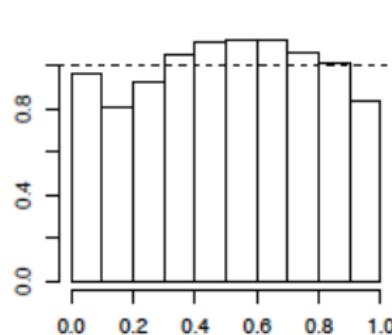
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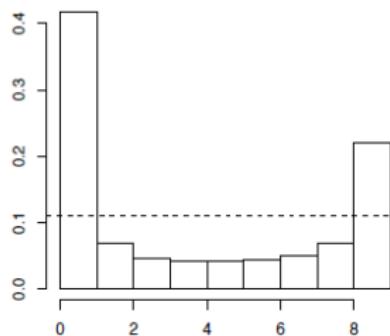
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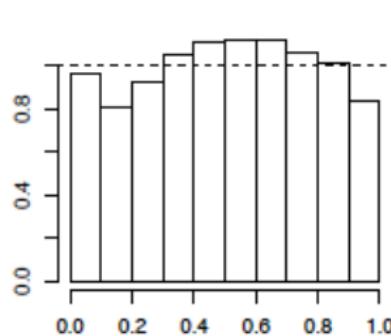
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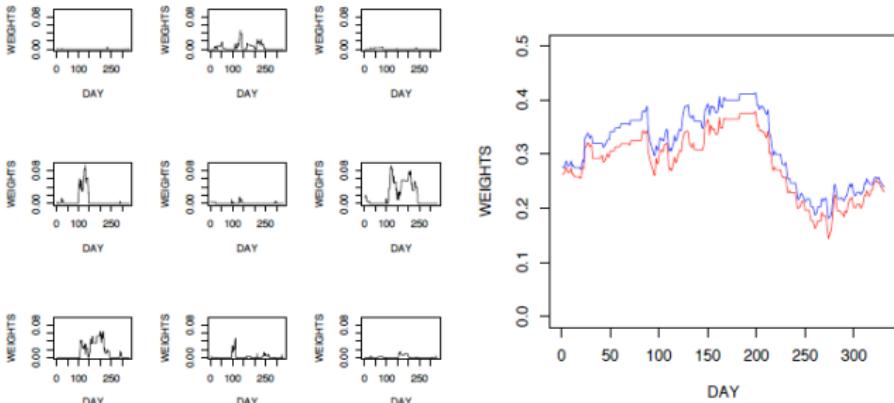
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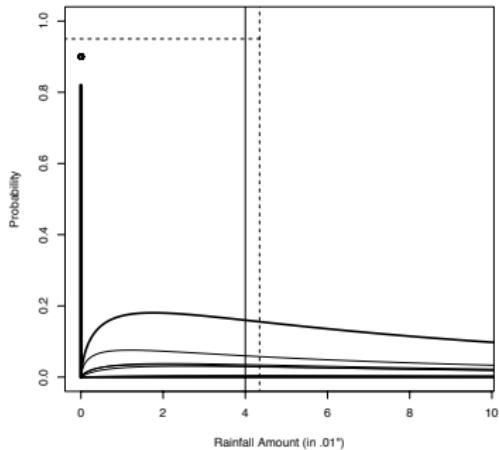
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- Recently extended to wind speeds:
  - **Zero component not needed in the Pacific Northwest**

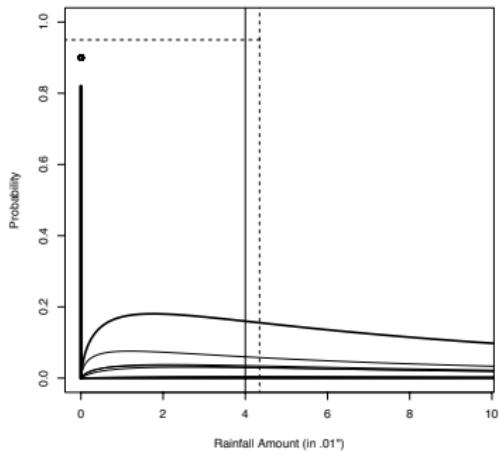
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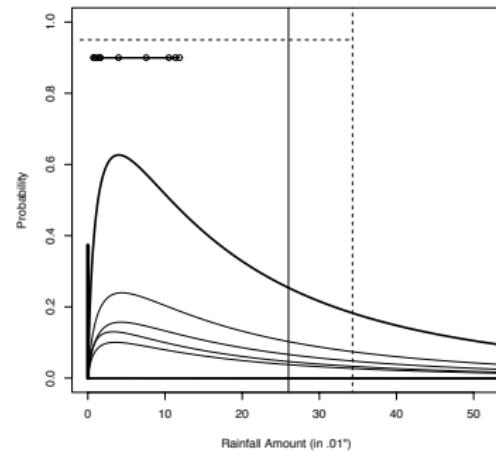


Renton, 19th May, 2003

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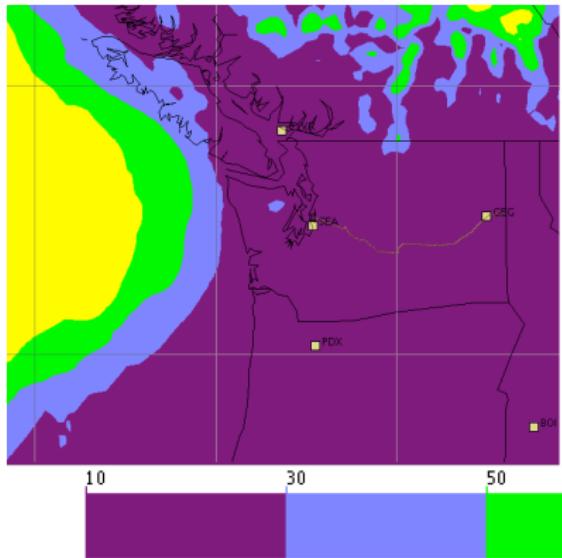
Renton, 19th May, 2003



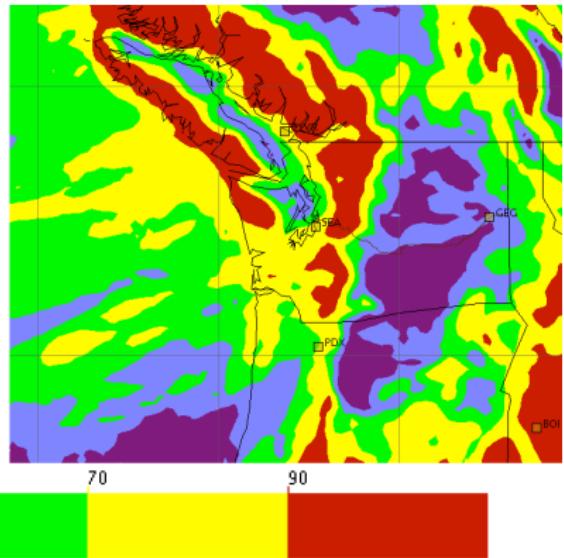
Station KPWT, 26th January, 2003

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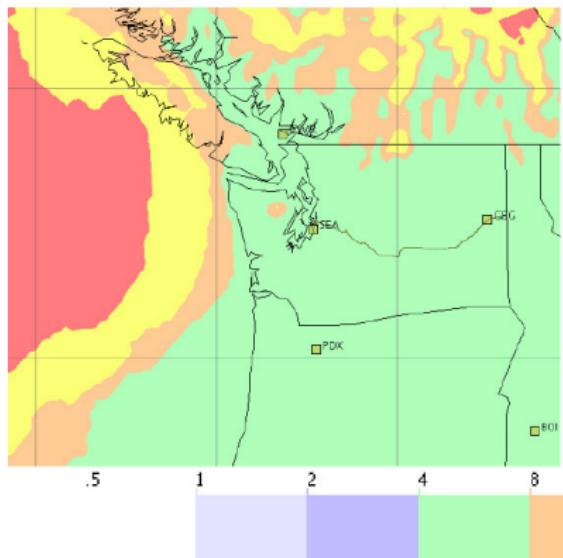
(a) 19th May, 2003



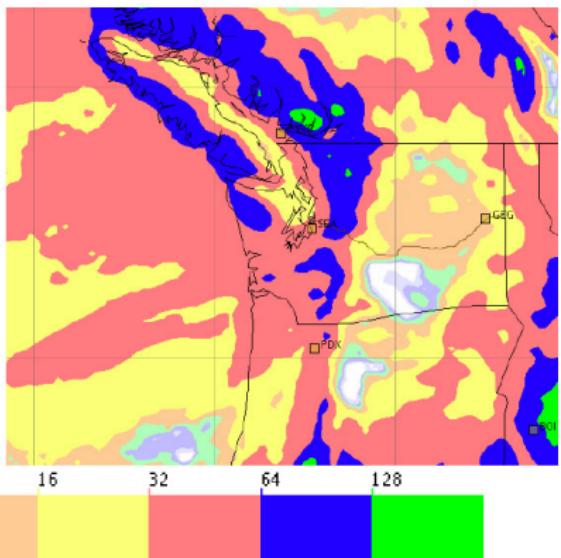
(b) 26th January, 2003

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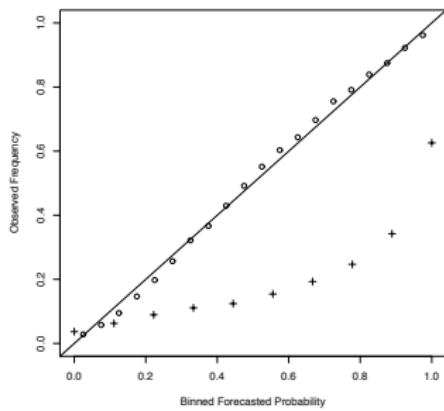
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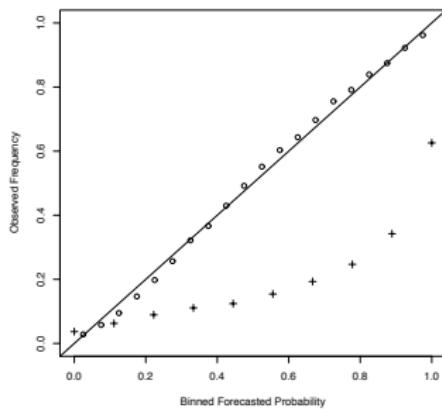
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# Calibration of Forecasts of the *Probability* of Precipitation

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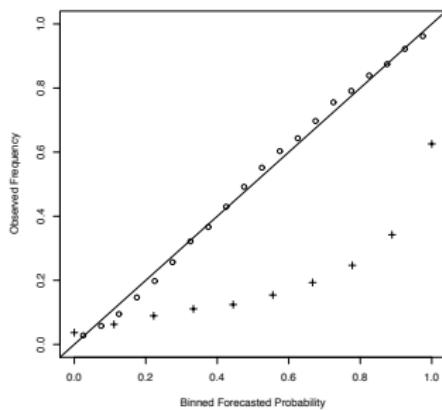


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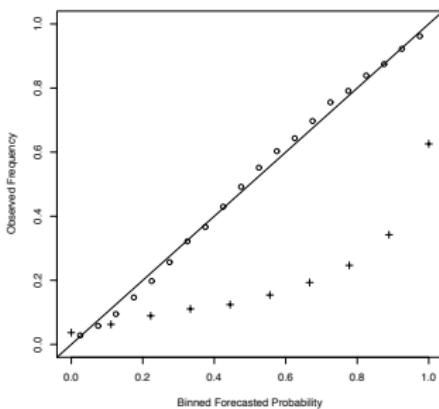
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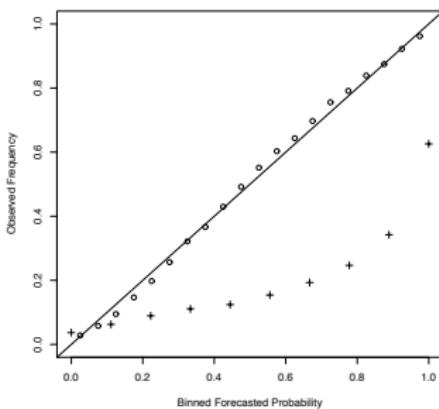
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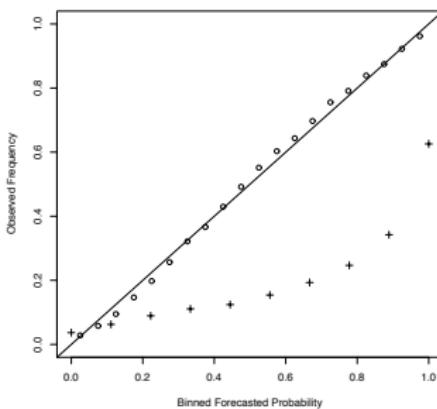
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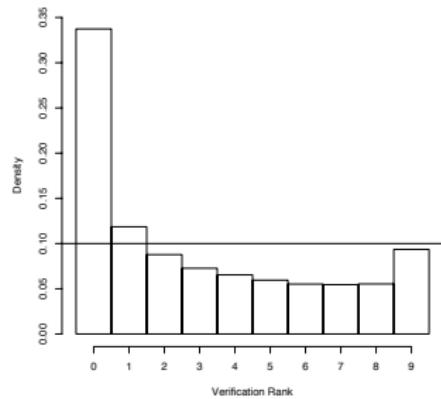
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- Circles show the BMA PoP forecast. Much better.

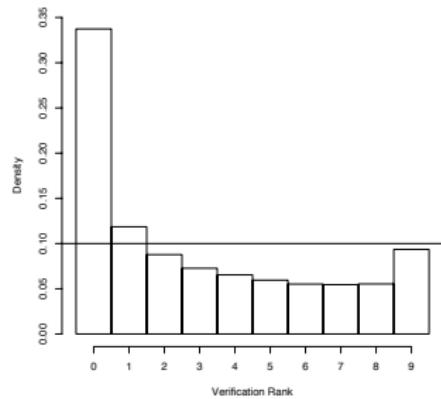
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Verification rank histogram  
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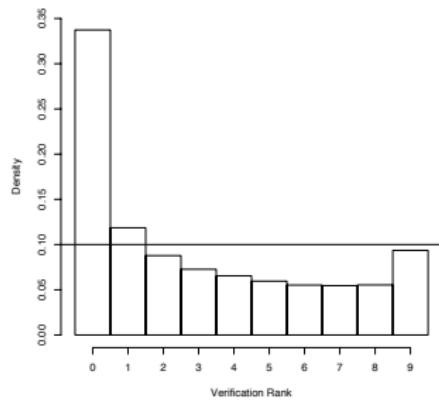
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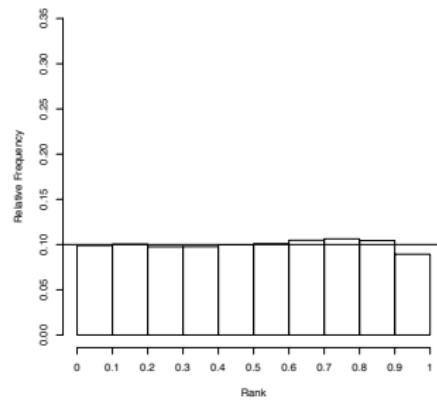
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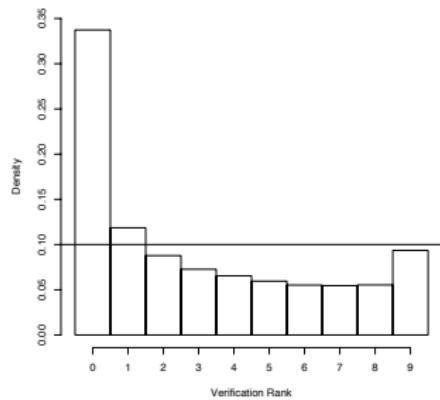
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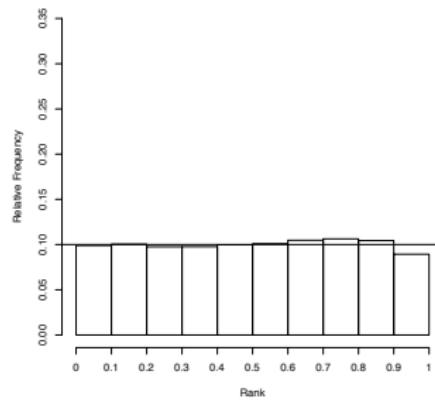
PIT histogram for  
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- $\Rightarrow$  **feasible to use BMA for the nation**

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  - **The result: the Geostatistical Output Perturbation (GOP) Method**

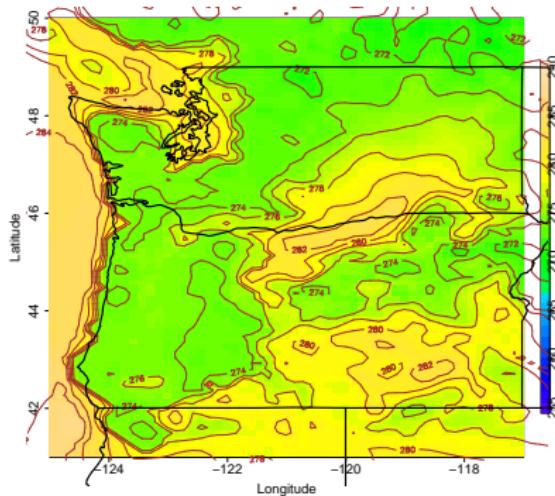
# Example

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Gridded Forecast for January 12, 2002

# Example

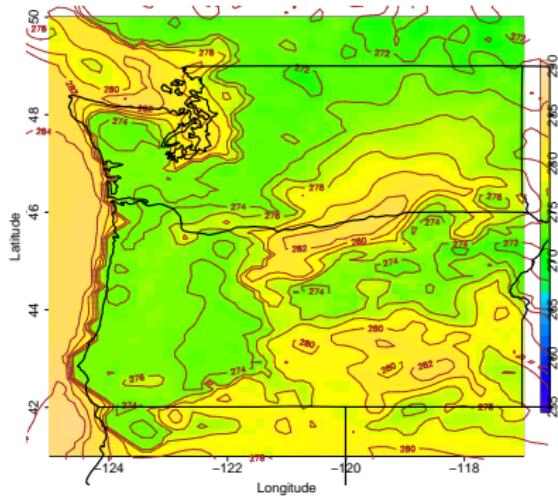
Gridded Forecast for January 12, 2002



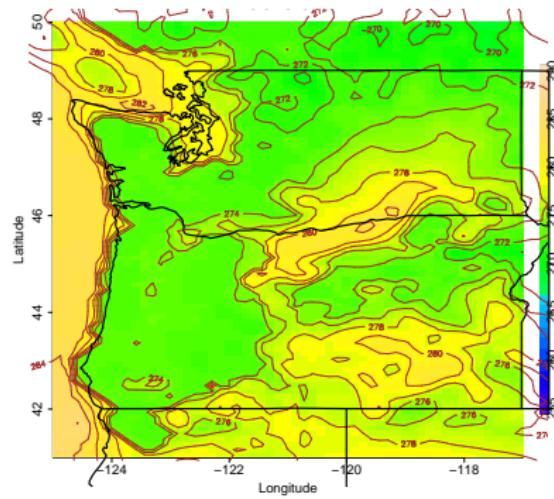
Gridded forecast

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Gridded Forecast for January 12, 2002



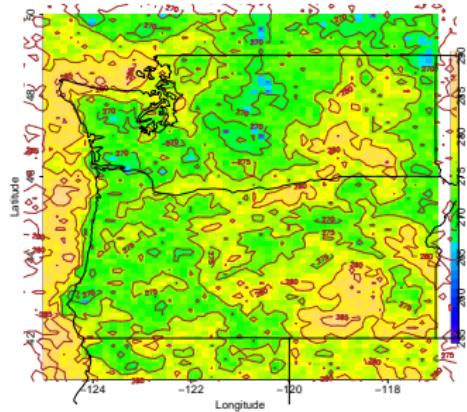
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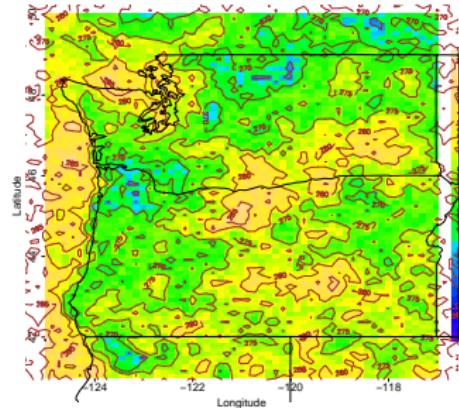
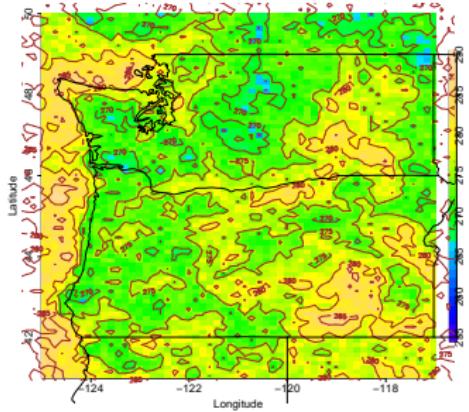
Bias-corrected

## Sample from the Forecast Predictive Distribution

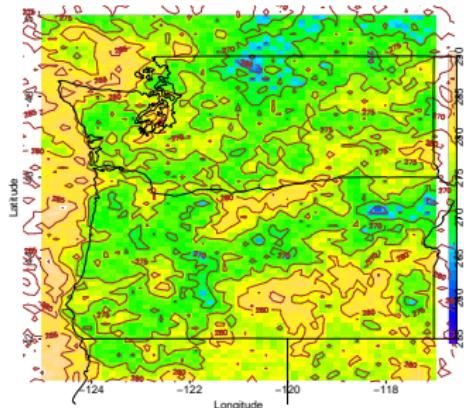
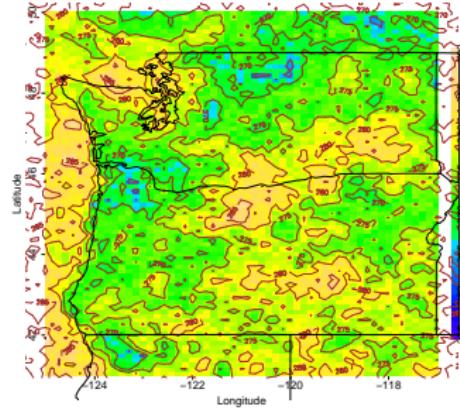
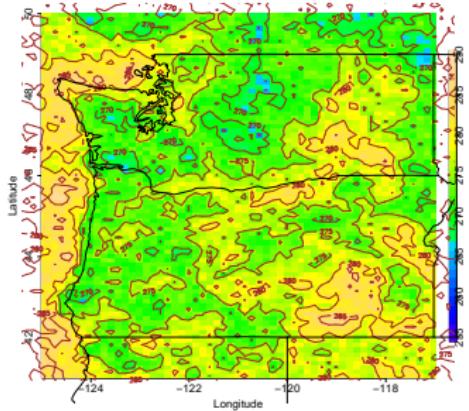
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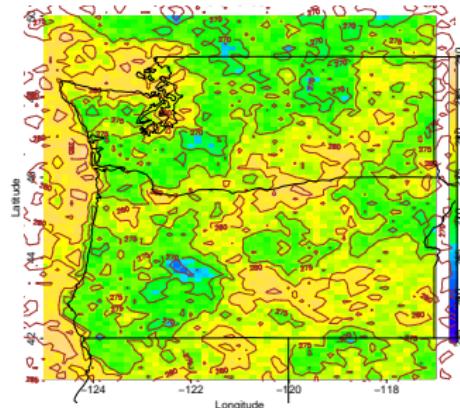
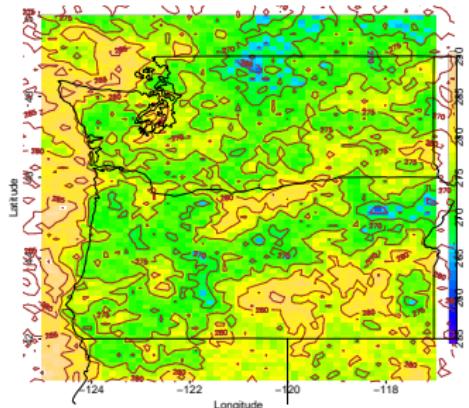
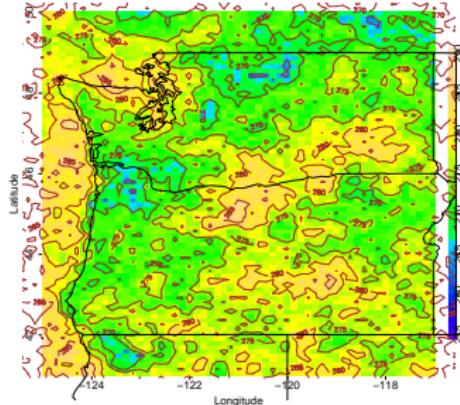
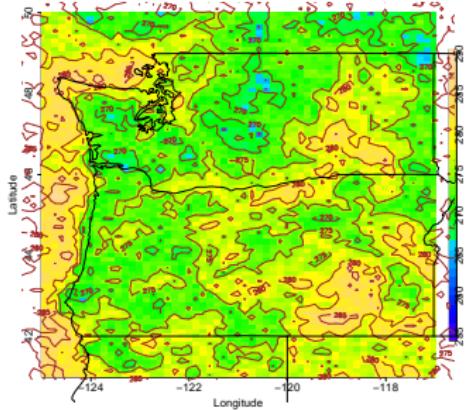
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