

1 Surface albedo feedback: comparison of model and
2 observational based estimates

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3 The ice albedo feedback (IAF) is the product of the ice sensitivity (IS) –
4 how much the sea ice concentration changes as the planet warms– and the
5 radiative sensitivity (RS) – how much the top of atmosphere radiation changes
6 as the surface albedo changes. We demonstrate that the RS calculated from
7 radiative kernels in climate models is reproduced from calculations that use
8 the climatological radiative fluxes at the top of atmosphere and the assump-
9 tion that the atmosphere is isotropic to shortwave radiation. This method
10 allows us to calculate RS from satellite based estimates of climatological ra-
11 diative fluxes and compare the resultant RS across a full suite of coupled cli-
12 mate models. We find that the model ensemble mean RS is very near that
13 constrained by the observations whereas the RS differs in climate models by
14 a factor of two in both the Arctic and Southern Ocean. Observed trends in
15 Arctic sea ice over the historical record are used to estimate IS which, in con-
16 junction with the satellite based RS calculates an IAF parameter of 0.13 W
17 $\text{m}^{-2} \text{ K}^{-1}$. This Arctic IAF would result in a modest amplification of future
18 global surface temperature change of approximately 11%.

1. Introduction

19 The reduction of sea ice area as the climate system warms darkens the surface resulting
20 in increased solar radiation absorbed in the climate system. This additional radiative input
21 reinforces the initial warming providing a positive climate feedback often termed the ice-
22 albedo feedback (IAF). Early literature on climate stability in simplified models speculated
23 that the IAF could cause abrupt and dramatic climate state transitions under smoothly
24 varying external forcing [Crowley and North, 1988; Budyko, 1969] and may even lead to the
25 existence of multiple climate state equilibria in more comprehensive coupled climate models
26 [Ferreira et al., 2011]. The role of the IAF in contemporary and future climate change
27 is expected to be more modest with model mean estimated feedback parameter of 0.3 W
28 $\text{m}^{-2}\text{K}^{-1}$ [Stocker et al., 2013; Bony et al., 2006; Soden and Held, 2006] which amounts to
29 approximately 30% enhancement of the global climate response to external forcing [Roe,
30 2009]. Observational estimates of the IAF using the co-variance of year-to-year sea ice
31 anomalies and satellite radiation suggest a similar magnitude (25% amplification of global
32 warming) IAF [Pistone et al., 2014]. However, there is substantial ($\pm 0.1 \text{ W m}^{-2}\text{K}^{-1}$)
33 inter-model spread in the strength of the IAF [Winton, 2006; Hall and Qu, 2006] and this
34 spread is understood to be the leading cause of inter-model differences in the high latitude
35 climate response to future warming [Hall, 2004; Kay et al., 2012] that varies substantially
36 between models [Holland and Bitz, 2003].

37 The magnitude of IAF depends on [Soden et al., 2008; Shell et al., 2008]: 1.) how much
38 sea ice concentration (SIC) reduces as the Earth warms ($\frac{dSIC}{dT_S}$), 2.) the surface albedo
39 contrast between open ocean and sea ice ($\Delta\alpha$) and, 3.) the impact of surface albedo

40 changes on top of atmosphere (TOA) radiation ($\frac{dRAD_{TOA}}{d\alpha}$) that we will hereafter refer to
 41 as radiative sensitivity (RS) :

$$IAF = \underbrace{\frac{dSIC}{dT_S}}_{IS} \Delta\alpha \underbrace{\frac{dRAD_{TOA}}{d\alpha}}_{RS}. \quad (1)$$

42 Hall and Qu [2006] found that the radiative impact of surface albedo anomalies on the
 43 TOA radiation – RS – varies very little between climate models. As a result, much of the
 44 literature on uncertainties in the IAF has focused on surface processes controlling the sea
 45 ice albedo and sensitivity of SIC to warming [Winton, 2006; Qu and Hall, 2005; Curry
 46 et al., 1994].

47 In this manuscript, we re-evaluate the inter-model spread in the sensitivity of TOA
 48 radiation to surface albedo changes (RS) and find this quantity differs by a factor of
 49 2 between climate models over both the Arctic and Southern Ocean (SO). RS depends
 50 primarily on cloud reflectivity; clouds impede the amount of downwelling solar radiation
 51 reaching the surface and also reduce the amount of solar radiation reflected by the sur-
 52 face from reaching the TOA [Taylor et al., 2007; Donohoe and Battisti, 2011] leading to
 53 a squared dependence of RS on cloud reflectivity. High latitude cloud properties vary
 54 substantially between climate models and exhibit biases relative to the observations in
 55 both the Arctic Gorodetskaya et al. [2006] and SO [Trenberth and Fasullo, 2010]. Thus,
 56 it is expected that the different mean state cloud fields simulated by each climate model
 57 results in different RS and that these inter-model differences will result in different model
 58 sensitivity of Arctic temperatures and sea ice concentrations to future warming [Hwang
 59 et al., 2011]. The primary goal of this manuscript is diagnosing these inter-model dif-

60 ferences in RS and using observational constraints to evaluate which models have IAFs
61 consistent with that in the observed climate system. A secondary goal is understanding
62 how much of the inter-model spread in RS contributes to model differences in IAF.

63 This manuscript is organized as follows: In section 2, we develop a simplified model
64 that allows the calculation of $\frac{dRAD_{TOA}}{d\alpha}$ (RS) from standard climate model output and
65 demonstrate that this method reproduces the results of much more computationally de-
66 manding radiative kernel techniques in the subset of models for which radiative kernel
67 calculations have been performed. This allows us to probe the large inter-model spread
68 of RS in the full ensemble of coupled climate models participating in the Coupled Model
69 Inter-comparison Project [CMIP Meehl et al., 2007; Taylor et al., 2012] and also provide
70 an observational estimate of RS from satellite data (Section 3). These estimates of RS
71 along with sea ice response over the historical period are used to calculate an observa-
72 tional IAF (Section 4). The observational IAF is compared to model estimates over both
73 the historical and 4XCO₂ simulations and the model spread and biases and decomposed
74 into contributions from radiative and sea ice sensitivity (Section 5). A summary and
75 discussion follows.

2. The impact of surface albedo changes on TOA radiation in radiative kernels and a simplified model

76 The impact of surface albedo changes on TOA radiation (RS) has been rigorously
77 calculated using radiative kernel techniques in a small number of climate models. Here,
78 we develop a secondary technique for calculating RS from climatological radiative fluxes
79 at the TOA and surface (standard climate model output fields) and a simple conceptual

80 model of shortwave radiation. We demonstrate that this simplified model reproduces the
81 domain average value of RS in the Arctic and SO, its spatial structure and inter-model
82 spread. Because this simplified technique calculates RS from climatological radiative
83 fluxes, satellite observations combined with surface radiation provide an observational
84 estimate of the RS.

2.1. Radiative kernels

85 RS can be calculated directly from offline radiative model calculations by perturbing
86 surface albedo (α) at each grid point and then running the radiative code with all other
87 fields unchanged – a technique referred to as radiative kernels [Soden et al., 2008; Shell
88 et al., 2008]. Radiative kernel calculations have been performed by the following individ-
89 uals/groups each using a different atmospheric model perturbed about a historical mean
90 state with seasonally varying prescribed sea surface temperatures: 1.) Karen Shell, NCAR
91 CAM3 [Shell et al., 2008], 2.) Karoline Block, MPI ECHAM6 [Block and Mauritsen, 2013],
92 3.) Angie Pendergrass, NCAR CAM5 [Pendergrass et al., 2018], 4.) Chris Smith, UKMO
93 HadGEM2 [Smith, 2018]. RS in the Arctic summer (May-June-July-August) is largest
94 over Greenland, smallest in the Greenland and Barents Sea and has intermediate values
95 in the central Arctic (Upper panels of Figure 1). This spatial structure primarily reflects
96 the climatological pattern of solar radiation reaching the surface in the Arctic [Lindsay
97 et al., 2014] with limited the high topography of Greenland having limited cloud cover
98 and water vapor in the overlying atmosphere, abundant clouds in the Greenland Sea and
99 moderate bur persistent cloud cover over the Central Arctic. RS has values of order 1.5
100 $\text{W m}^{-2} \%^{-1}$ over the Arctic Ocean. The summertime average insolation over this region

101 is of order 420 W m^{-2} . Thus, one would expect a RS $4.2 \text{ W m}^{-2} \%^{-1}$ in a completely
102 transparent atmosphere. On average, the atmosphere attenuates the surface contribution
103 to reflected radiation at the TOA by a factor of 3 consistent with the finding of Donohoe
104 and Battisti [2011].

105 There is remarkable inter-model spread in Arctic RS across the different radiative kernel
106 calculations, especially over the Central Arctic where the calculations in the different
107 climate models differ by a factor of 2. Domain average values (poleward of 60°N are
108 shown in the upper right corner of the panels in Figure 1 and also differ by a factor of 2.
109 Interestingly, the end member values of RS come from the same modeling center (NCAR)
110 using different generations of the atmospheric model (CAM5 versus CAM3). Additional
111 radiative kernels are available from Brian Soden’s calculations in GFDL AM2p12b [Soden
112 et al., 2008] and Michael Previdi’s calculation in MPI ECHAM5 [Previdi, 2010] and are
113 not shown here because the climatological radiative fields that we will use in the next
114 subsection were not saved. These additional models have RS generally within the range
115 covered by those shown in Figure 1.

116 In the SO, RS during the Austral summer (NDJF) calculated from radiative kernels
117 shows an annular (i.e. nearly zonally homogenous) structure in all models with smaller
118 values over the cloudy storm track region equatorward of the ice edge and larger values
119 over the ice (upper panels of Figure 2). However, the models differ to first order on the
120 magnitude of RS over the open ocean and on the location of the and aerial extent of the
121 region of larger RS adjacent to the Antarctic continent. In HADGEM2, the value of RS
122 over the open ocean is $2 \text{ W m}^{-2} \%^{-1}$ whereas in NCAR CAM3 RS is $1 \text{ W m}^{-2} \%^{-1}$ over

123 the same region. In NCAR CAM5, the region of high RS adjacent to the Antarctic coast
124 extends substantially into the SO whereas in NCAR CAM3 and ECHAM6 the same the
125 high RS region is confined to coast itself with the exception of the Weddel and Ross Seas.
126 These inter-model differences in the region of high RS correspond to inter-model biases
127 in summertime ice extent. Overall, the SO domain average RS (excluding the Antarctic
128 continent) ranges from 1.29 to 1.75 $\text{W m}^{-2} \%^{-1}$ (as shown by the values in the upper right
129 corner of Figure 2). This domain average inter-model spread in RS is smaller than that
130 over the Arctic in the same models, but still amounts to about 40% of the mean value.

2.2. Isotropic single layer model

131 We now present an alternative simplified method for calculating RS from the climatolog-
132 ical radiative fluxes at the TOA and surface only and some basic simplifying assumptions
133 about shortwave radiative transfer in the atmosphere. We begin by describing the as-
134 sumptions that we will refer to as the isotropic model which was developed by Taylor
135 et al. [2007] and will then describe how this model allows the calculation of RS. Of the
136 incident shortwave radiation at the TOA (S), we assume that a fraction (A) is absorbed
137 in the atmosphere above cloud top and a fraction R of the radiation incident on cloud top
138 is reflected back to space (Figure 3). This resultant downwelling radiation at the surface
139 is $S(1-A)(1-R)$. A fraction (α) given by the surface albedo of the surface downwelling is
140 reflected upwards. R of the surface upwelling radiation is reflected back (downward) to
141 surface with the remainder ($S[1-A][1-R]^2$) transmitted to space. Reflections and trans-
142 missions are continued indefinitely subject to the two primary assumptions: 1. cloud
143 reflection is isotropic – the same fraction (R) of broadband shortwave radiation incident

144 on the cloud layer is reflected independent of the direction (upwelling/downwelling) and
 145 how many previous interactions with the surface and cloud occur and 2. all of the atmo-
 146 spheric absorption occurs above cloud top which is apt for describing SW absorption by
 147 ozone in the stratosphere.

148 In the above model, loss of radiative energy from the climate system due to surface
 149 albedo is a three step process: 1. insolation must be transmitted to the surface then
 150 2. reflected by the surface and finally 3. transmitted from the surface to the TOA. In
 151 symbolic terms, upwelling SW radiation at the TOA that results from reflection off the
 152 surface is equal to the insolation (S) times the downwelling transmissivity ($[1 - A] [1 - R]$)
 153 times the upwelling transmissivity (1-R). Higher order reflections where the SW radiation
 154 reflected at the surface is reflected back to the surface off clouds and thereafter will
 155 contribute additional upwelling SW fluxes at the TOA with each subsequent reflection
 156 equal to the value of the previous order contribution times αR . These terms form an
 157 infinite geometric series that converges to :

$$SW \uparrow_{TOA} = \underbrace{SR(1-A)}_{SW \uparrow_{TOA,atmos}} + S\alpha \underbrace{\frac{(1-A)(1-R)^2}{1-\alpha R}}_{SW \uparrow_{TOA,surf}}, \quad (2)$$

158 where $SW \uparrow_{TOA,atmos}$ and $SW \uparrow_{TOA,surf}$ indicates the upwelling radiation at the TOA that
 159 was derived from atmospheric and surface reflection respectively. Thus, if the values
 160 of R and A along with α and S are known, the contribution of the surface to the SW
 161 flux at the TOA can be calculated. In our case, we know the upwelling and downwelling
 162 radiative fluxes at the TOA and surface (4 variables) and we have four unknowns (A,R,S, α)
 163 resulting in a determined set of equations. Thus, the climatological radiative fluxes allow

164 the calculation of the single pass A and R for each climate model. We can then calculate
 165 the expected change of $SW \uparrow_{TOA}$ as α changes with all is being equal by taking the partial
 166 derivative is Eq. 2 with respect to α .

$$\frac{\partial SW \uparrow_{TOA}}{\partial \alpha} = S \frac{(1 - A)(1 - R)^2}{1 - \alpha R} \left(1 + \frac{R\alpha}{1 - R\alpha} \right). \quad (3)$$

167 Eq. 3 is an alternative calculation of RS that relies only on climatological data and can be
 168 compared with the RS calculated from offline radiative kernel techniques. In this frame-
 169 work, RS consists of two terms. The first term equals the climatological $SW \uparrow_{TOA,surf}$
 170 times the fractional α change and is the product of the climatological downwelling and
 171 upwelling atmospheric transmissivity modified by a factor to account for multiple reflec-
 172 tions by the climatological α . The second term includes the impact of the modified α on
 173 secondary and thereafter reflections and tends to be substantially smaller than the first
 174 term except over regions that are both ice covered and cloudy.

175 The lower panels of Fig. 1 show the RS in the Arctic summer calculated from Eq. 3
 176 applied to the climatological fields in the same simulations used to calculate the radiative
 177 kernels. The RS calculated from the isotropic model and radiative kernels are in excellent
 178 agreement; the spatial correlation within each model has an R^2 that exceeds 95% in all but
 179 NCAR CAM3 and the inter-model differences in domain average and regional patterns of
 180 RS are nearly identical in the isotropic model and radiative kernel estimates of RS (c.f.
 181 the adjacent upper and lower panels of Fig. 1 with R^2 listed in the middle). Similarly,
 182 in the SO the isotropic model captures the spatial pattern and inter-model spread of RS
 183 very well (Fig. 2). Overall, these results suggest that the isotropic model captures the

184 essential SW radiative processes that determine the RS of surface albedo changes and
185 that the inter-model spread in RS is determined by the climatological cloud reflectivity
186 which is adequately calculated from the climatological TOA and surface fluxes according
187 to Eq. 2. The isotropic model tends to bias the RS high relative to the radiative kernel
188 (c.f. the domain average values listed in the upper right of the map in the upper and lower
189 panels of Figs. 1 and 2) and we speculate this results from the simplifying assumption
190 that atmospheric absorption only occurs during the first pass as this allows more of the
191 radiation reflected off the surface to be transmitted to space than would occur if the atmo-
192 sphere absorbed upwelling solar radiation. Alternative formulations of similar isotropic
193 models [Donohoe and Battisti, 2011] assume the atmospheric absorption occurs in the
194 same layer as the cloud reflection and occurs on all passes through the atmosphere to
195 account for shortwave absorption by water vapor that occurs throughout the troposphere
196 Donohoe and Battisti [2013]. This model better matches the RS calculated by radiative
197 kernels in the tropics and mid-latitudes but substantially underestimates the radiative
198 kernel derived RS in the high-latitudes (not shown). We speculate that in the dry Arctic,
199 the atmospheric absorption is primarily by stratospheric ozone whereas in the lower lati-
200 tudes water vapor also contributes. For this reason, we choose to assume the absorption
201 occurs only on the downward pass and return to possible impacts and improvements of
202 this method in the discussion section.

3. Observational estimate of radiative sensitivity to surface albedo changes and comparison to coupled models

203 Given the excellent correspondence between RS calculated from radiative kernels and
204 the isotropic model (Figs 1 and 2), we can use the isotropic model to calculate RS from
205 observational estimates of radiative fluxes at the TOA and surface and from the same
206 fields that are commonly exported from standardized [Taylor et al., 2012] climate model
207 simulations. This procedure allows RS to be determined across a broad range of models
208 and to compared with the observational estimates to assess model biases in how sensitivity
209 the radiative budget of the climate system is to ice loss.

210 Observational estimates of climatological radiative fluxes are taken from the CERES
211 EBAF surface product version 4.0 [Loeb et al., 2018; Kato et al., 2018] that covers the time
212 period March of 2000 to March 2018. For purposes of comparison with the observations,
213 we use calculate RS in climate models using the isotropic model applied to climatological
214 radiative fluxes from the last decade (1995-2005) of historical CMIP5 [Taylor et al., 2012]
215 climate simulations forced by observed greenhouse gases. Most of the radiative kernel cal-
216 culation discussed in Section 2 were initialized from “modern day” but the exact definition
217 differs between models in part due to the different time the calculations were performed.

218 The observational estimate of RS averaged over the Arctic during summer is 1.79 W
219 $\text{m}^{-2} \text{ \%}^{-1}$ over the whole domain and $0.86 \text{ W m}^{-2} \text{ \%}^{-1}$ averaged over the ocean only (Fig.
220 4). The observational RS is very similar to the historical model ensemble mean (1.72 and
221 $0.87 \text{ W m}^{-2} \text{ \%}^{-1}$ over the entire Arctic domain and ocean only respectively). The models
222 and observations generally agree on the spatial pattern of RS over the Arctic with high
223 values over the Greenland ice sheet where the reduced mass of the atmosphere above the

224 topography is associated with enhanced atmospheric SW transmissivity, lower RS values
225 over the Norwegian Sea and more spatially uniform RS values over the Central Arctic.
226 However, the magnitude of RS differs substantially across models with domain average
227 RS differing by almost a factor of two between the models with the smallest and largest
228 RS.

229 Similarly, in the SO the observational estimate of summertime (NDJF) RS is similar
230 but slightly lower (domain average excluding the Antarctic continent of $1.56 \text{ W m}^{-2} \%^{-1}$)
231 than the ensemble mean ($1.71 \text{ W m}^{-2} \%^{-1}$). All models and observations agree that the
232 RS has a mostly annular structure with smaller values in the storm track region and larger
233 values adjacent to the Antarctic continent over the sea ice. However, the models differ
234 substantially (order factor 2) on the magnitude of RS in the storm track region and on
235 the location and lateral extent of the high RS region adjacent to the continent. Some
236 models (i.e. CSIRO MK5) also have zonal asymmetries in RS that are best characterized
237 as a zonal wavenumber 1 pattern. The domain average RS values differ by less than the
238 factor of 2 differences seen in the Arctic, but the local RS difference between models –
239 especially in the storm track region – are of order a factor of 2. These results collectively
240 suggest that while the CMIP5 ensemble average RS of high latitude ice loss is very near
241 that implied from observational constraints, models diverge substantially on the radiative
242 impact of ice loss due to their climatological atmospheric optical properties (i.e. clouds).
243 We now analyze how these inter-model differences in RS impact the magnitude of the IAF
244 and consider how much the IAF amplifies global warming in the observed climate system
245 and in models

4. Observational estimate of ice albedo feedback and comparison to coupled models

246 The ice albedo feedback (IAF) is the product of the RS – the TOA radiative impact to
247 surface albedo changes – and the ice sensitivity (IS) – the surface albedo change due to ice
248 loss per unit of global warming (Eq. 1). Thus, the RS calculated from the climatological
249 radiative fluxes and the isotropic model in the previous sections along with estimates of
250 IS from the observational record provide an observational estimate of the IAF that can
251 be compared to the IAF calculated using the same methodology applied to climate
252 model simulations of historical and long term forcing. Furthermore, we can explicitly ask
253 if the model spread (and potential bias relative to observations) in IAF is due to RS or
254 IS differences.

255 The observational estimate of IS is calculated from the changes in decadal average sea ice
256 concentration between 1979 and present day (2007-2016 average minus 1979-1988 average
257 – Fig. 6). This time period is chosen to coincide with the coverage of the Nimbus 7 satellite
258 that provides the passive microwave brightness used to calculate sea ice concentration by
259 the National Snow and Ice Data Center [Cavalieri et al., 1996]. Monthly maps of the
260 decadal average change in sea ice concentration are multiplied by an assumed surface
261 albedo contrast between the open ocean and sea ice ($\Delta\alpha$) of 0.54 -assuming a typical ice
262 α of 0.6 [Hummel and Reck, 1979] and an ocean albedo of 0.06 [Hansen et al., 2013] and
263 then normalized by a global surface temperature change of 0.7K over this time period
264 [Hansen et al., 1999; Morice et al., 2012]. The monthly IS is then multiplied by the
265 monthly RS derived from CERES data then time averaged to produce a map of radiative
266 impact of sea ice changes. We have shown the raw (not normalized by global temperature

change) radiative impact averaged over the summer months (MJJAS) in Fig.6 which has
an Arctic domain average of 3.4 W m^{-2} . To convert this number to a global and annual
mean radiative impact, one must dilute this number by the ratio of summer months to the
year ($\frac{4}{12}$) and the spatial area of the Arctic (poleward of 60°N) divided by that of the globe
(.065) resulting in a global radiative impact of 0.091 W m^{-2} . This translates to a global
radiative feedback of $0.13 \text{ W m}^{-2} \text{ K}^{-1}$ given the observed global surface temperature
change over the same period. We do not estimate the surface albedo feedback in the
SO because the change in SO sea ice concentration over the observational period is not
statistically significant above the year-to-year variability [Jones et al., 2016].

We now compare the observational Arctic IAF derived above with that derived by
the same procedure in historical CMIP5 simulations. The RS for each climate model
that was calculated in the previous section (from the climatology at end of the historical
simulation – 1995 to 2005) is multiplied by the decadal average surface albedo change over
the historical simulation (1995 to 2005 minus 1975 to 1985). The RS and surface albedo
changes are calculated for each month. For simplicity, we will only discuss the annual
mean of the calculations projected onto the global impact normalized by the global mean
surface temperature change over the same time period. The ensemble average Arctic IAF
in the historical simulations is $.14 \text{ W m}^{-2} \text{ K}^{-1}$ with a spread (2 standard deviations, σ)
of $0.18 \text{ W m}^{-2} \text{ K}^{-1}$ (black histogram in upper left panel of Fig. 7). The ensemble mean
is very close to the observational estimate (c.f the solid and dashed vertical black lines in
Fig. 7) but the large inter-model spread indicates that the models differ in either their

288 RS or IS and we now ask how much RS and IS contribute to the inter-model differences
289 in Arctic IAF.

290 To answer how much the IS contributes to the IAF spread, we repeat the calculation of
291 IAF as the time and spatial average of the product of RS and IS but, instead of using the
292 model specific RS, we replace the RS in all models by the observational based RS. The
293 resultant distribution of IAF (blue histogram in Fig. 7) shows the IAF spread that would
294 result if all models had the observed RS and indicates the role of inter-model spread of IS
295 (and potentially the bias) in determining the IAF. We see that the mean of distribution
296 is nearly equal to that of the full IAF calculation (c.f. the blue and black vertical lines)
297 indicating that the ensemble average IS is very similar to that observed. Furthermore,
298 the spread in the fixed RS distribution is only slightly smaller than that of the full IAF
299 calculation ($2\sigma = 0.16 \text{ W m}^{-2} \text{ K}^{-1}$) indicating that the majority of the inter-model spread
300 in IAF calculated from the historical simulation is a result of the IS differences between
301 models.

302 Similarly, we can assess the impact of inter-model RS differences (and biases) on the
303 calculated IAF by replacing the model specific IS with that derived from the observations
304 (red histogram in Fig.7). The ensemble average IAF of the fixed IS distribution is nearly
305 identical to that of the full IAF calculation (c.f. the red and black vertical lines in Fig.
306 7) indicating that the ensemble average RS is similar to that calculated from the CERES
307 data. The inter-model spread in IAF in the fixed IS experiment ($2\sigma = 0.05 \text{ W m}^{-2}$
308 K^{-1}) is smaller than that of the full calculation and fixed RS experiment indicating that

309 inter-model differences in RS play a smaller but not insignificant role in the IAF spread
310 calculated over the historical simulations.

311 The above partitioning of IAF into differences in RS and IS take into account the
312 spatial and temporal co-variances of ice loss and RS by weighting the ice loss to the RS
313 at that location and time. Similar results for the impact of IS and RS on the total spread
314 in calculated IAF are obtained by simply noting the fractional spread (relative to the
315 ensemble mean) of summertime Arctic domain average RS and IS between models. The
316 ratio of 2σ to the ensemble mean value of RS is 40% whereas that of IS is 107% roughly
317 scaling with the fractional contribution to IAF spread calculated above.

318 The sea ice retreat over the historical record represents the superposition of the response
319 to climate forcing and natural variability and, thus, the inter-model spread in IS calcu-
320 lated over the 30 years of historical simulations is expected to exceed that in response to
321 long-term forcing. Studies suggest that 60% of the observed Arctic sea loss since 1979
322 is a result of the natural variability of atmospheric circulation [Ding et al., 2017] and
323 that trends in sea ice differ by as much as 50% at the multi-decadal timescale in model
324 ensembles due to natural variability [Kay et al., 2011]. For these reason, we also look
325 at the contribution of RS and IS to the inter-model spread in the IAF in response to
326 an abrupt and sustained quadrupling of atmospheric CO_2 . The ensemble average Arctic
327 IAF calculated from the 4XCO_2 simulations is $0.13 \pm 0.10 \text{ W m}^{-2} \text{ K}^{-1}$ (uncertainty is
328 2σ) and is in close agreement with the observational estimate ($0.13 \text{ W m}^{-2} \text{ K}^{-1}$) and the
329 ensemble average of the historical simulation ($0.14 \text{ W m}^{-2} \text{ K}^{-1}$). When the model specific
330 RS is replaced by the observational estimate of RS the resultant Arctic IAF is 0.13 ± 0.08

331 $\text{W m}^{-2} \text{K}^{-1}$ and when the model specific IS is replaced by the observational estimate
332 of IS the resultant IAF is $0.13 \pm 0.04 \text{ W m}^{-2} \text{K}^{-1}$ (lower left panel of Fig. 7). These
333 results suggest that, in the long-term response to sustained anthropogenic forcing: 1.) the
334 CMIP5 ensemble average RS (spatially and temporally weighted by the relevant regions
335 of ice loss) is very near the observational estimate, 2.) the CMIP5 ensemble average IS
336 (spatially and temporally weighted by structure of RS) is very near the observational es-
337 timate and 3.) inter-model differences in IS contribute twice as much to the inter-model
338 spread in IAF (63% of the ensemble average value) than do inter-model differences in RS
339 (30% of the ensemble average value). We note that, the inter-model spread in IS and RS
340 are significantly ($R=0.54$) correlated and we return to the implication of this result in the
341 discussion section.

342 We repeat the analysis of the simulated IAF under 4XCO_2 in the SO (poleward of 55°S)
343 and find an ensemble average IAF of $0.06 \pm 0.11 \text{ W m}^{-2} \text{K}^{-1}$ (lower right panel of Fig.
344 7). When the model specific RS is replaced by the observational estimate of RS, the
345 calculated SO IAF is $0.05 \pm 0.09 \text{ W m}^{-2} \text{K}^{-1}$ suggesting the the ensemble average RS
346 is slightly larger than that estimated from the observations which is consistent with Fig.
347 5. Because we have no observational estimate of SO IS, we probe the sensitivity of SO
348 IAF to RS by replacing the model specific IS with the ensemble average IS resulting in
349 a calculated IAF of $0.06 \pm 0.03 \text{ W m}^{-2} \text{K}^{-1}$. This result suggest that while inter-model
350 differences in RS alone result in inter-model differences in SO IAF that are of magnitude
351 50% of the ensemble mean estimate, this contribution is dwarfed by the impact of inter-
352 model differences in IS which result in the inter-model differences in SO IAF exceeding

353 the central estimate by almost a factor of 2 (180%). This result is consistent with the
354 large inter-model differences in SO ice response to global warming reported by Shu et al.
355 [2015]; Polvani and Smith [2013].

5. Summary and discussion

356 We have shown that the radiative impact of surface albedo changes (RS) that is calcu-
357 lated from offline radiative transfer models (radiative kernels) can be very nearly replicated
358 from calculations with a simplified single layer isotropic SW radiation model applied to
359 the climatological radiative fluxes at the TOA and surface and a . This procedure allows
360 the IAF to be calculated from observational based data sets and standard monthly mean
361 climate model output allowing a comparison of observational and model estimates of IAF
362 as well as a decomposition of the model bias and inter-model spread into contribution
363 from RS and ice sensitivity (IS). The RS in climate models is, on average, very near the
364 observational estimate in the Arctic and only slightly larger than the observational esti-
365 mate in the SO. However, the inter-model spread in RS (Figs. 4 and 5) is substantial
366 in the absolute sense and results in inter-model differences that are 30% and 50% the
367 magnitude of the ensemble mean IAF in the Arctic and SO respectively.

368 Our results indicate that inter-model differences in IS contribute more to the inter-model
369 spread in IAF than does RS. However, IS is not independent of RS in the statistical sense
370 ($R = 0.54$) as one would expect on physical grounds whereby models that have a larger
371 radiative response to sea ice loss will tend to have larger sea ice loss due to a stronger
372 positive feedback between some initial ice loss and radiative energy gain in the climate
373 system. In this the sense, the contribution of RS to inter-model differences of 0.04 and

374 $0.03 \text{ W m}^{-2} \text{ K}^{-1}$) in the Arctic and SO respectively can be thought of as a lower bound
375 on the contribution of mean state radiative biases to the IAF. We hope to explore the
376 impact of mean state radiative biases (RS) on IS and the persistence of sea ice loss events
377 in future work.

378 We calculate an observational based Arctic surface albedo feedback of $.13 \text{ W m}^{-2} \text{ K}^{-1}$
379 from the product of the historical trend sea ice trend from 1979 to present day and the
380 CERES derived radiative sensitivity (RS). This result is substantially smaller than the
381 value of $0.31 \pm 0.04 \text{ W m}^{-2} \text{ K}^{-1}$ calculated by Pistone et al. [2014] from the covariance
382 of sea ice concentration and TOA radiation measured by CERES extrapolated to the sea
383 ice loss over nearly the same time period (1979-present day) analyzed in this work. We
384 speculate that some of the TOA radiative variability that coincides with ice loss events in
385 Pistone et al. [2014] is not directly a consequence of (i.e. geographically co-located with
386 and/or a radiative consequence) of surface albedo changes but, rather, is a consequence
387 of atmospheric optical properties (i.e. clouds, water vapor, etc) that co-vary with Arctic
388 sea ice concentration. A central question moving forward is whether the atmospheric
389 changes (and the associated radiative anomalies) accompanying Arctic sea ice loss over
390 the limited historical period result from natural variability of atmospheric circulation
391 initiated by tropical and mid-latitude processes or are a direct result of sea ice loss and,
392 thus, should be expected also apply to future climatological changes. We emphasize that
393 our observational estimate of the IAF is physically confined to the regions of ice changes
394 and is well validated by comparison to radiative kernels such that the primary uncertainty
395 in our calculation rests on how accurately the IS over the historic record represents the

396 expected relationship between future changes in Arctic ice concentration and global mean
 397 temperature.

398 Pistone et al. [2014] suggest that the IAF alone results in a 25% enhancement of global
 399 warming via radiative feedbacks a value they derive from the ratio of their calculated
 400 radiative impact of historic ice loss divided by the anthropogenic climate forcing to date.
 401 We offer two modifications to their calculation: 1. a significantly lower estimate of the
 402 radiative impact of Arctic sea ice loss outlined above and 2. consideration of how the
 403 implied feedback relates to equilibrium climate sensitivity, noting that climate system
 404 is not currently in equilibrium with the anthropogenic forcing to date. For the latter
 405 reason, the feedback gain of the Arctic IAF should be calculated by comparing the IAF
 406 to the equilibrium radiative feedback of all other radiative processes as opposed to the
 407 ratio of the transient radiative impact of ice loss to date to the applied forcing. Given
 408 observational central estimates of the total equilibrium feedback parameter of -1.19 W
 409 $\text{m}^{-2} \text{K}^{-1}$ [Armour, 2017] and our observational estimate of the Arctic IAF ($\lambda_{IAF} = +0.13$
 410 $\text{W m}^{-2} \text{K}^{-1}$) the implied feedback parameter of all processes excluding the IAF (λ_0) is
 411 $-1.32 \text{ W m}^{-2} \text{K}^{-1}$. The fractional amplification of global mean temperature changes – the
 412 feedback gain, G_{IAF} – due to the IAF is then [Roe, 2009]:

$$G_{IAF} = \frac{1}{1 + \frac{\lambda_{IAF}}{\lambda_0}} = 1.11. \quad (4)$$

413 Thus, our analysis suggest that the Arctic IAF amplifies global warming by 11% at the
 414 equilibrium timescale and is a more modest amplifier of global warming than the 25%
 415 suggested by Pistone et al. [2014].

Appendix A: Supporting Information

416 **Acknowledgments.** We thank Angeline Pendergrass, Chris Smith, Ryan Kramer,
417 Karen Shell, Brian Soden, Block and Marotzke and Michael Previdi for providing ra-
418 diative kernel calculation and their assistance providing further clarification on the ap-
419 propriate climatological radiation fields to use for isotropic model calculations. This work
420 was funded by a Department of energy mini grant to the HLES team at PNNL and the
421 NSF Antarctic Program Grant Number PLR 1643436.

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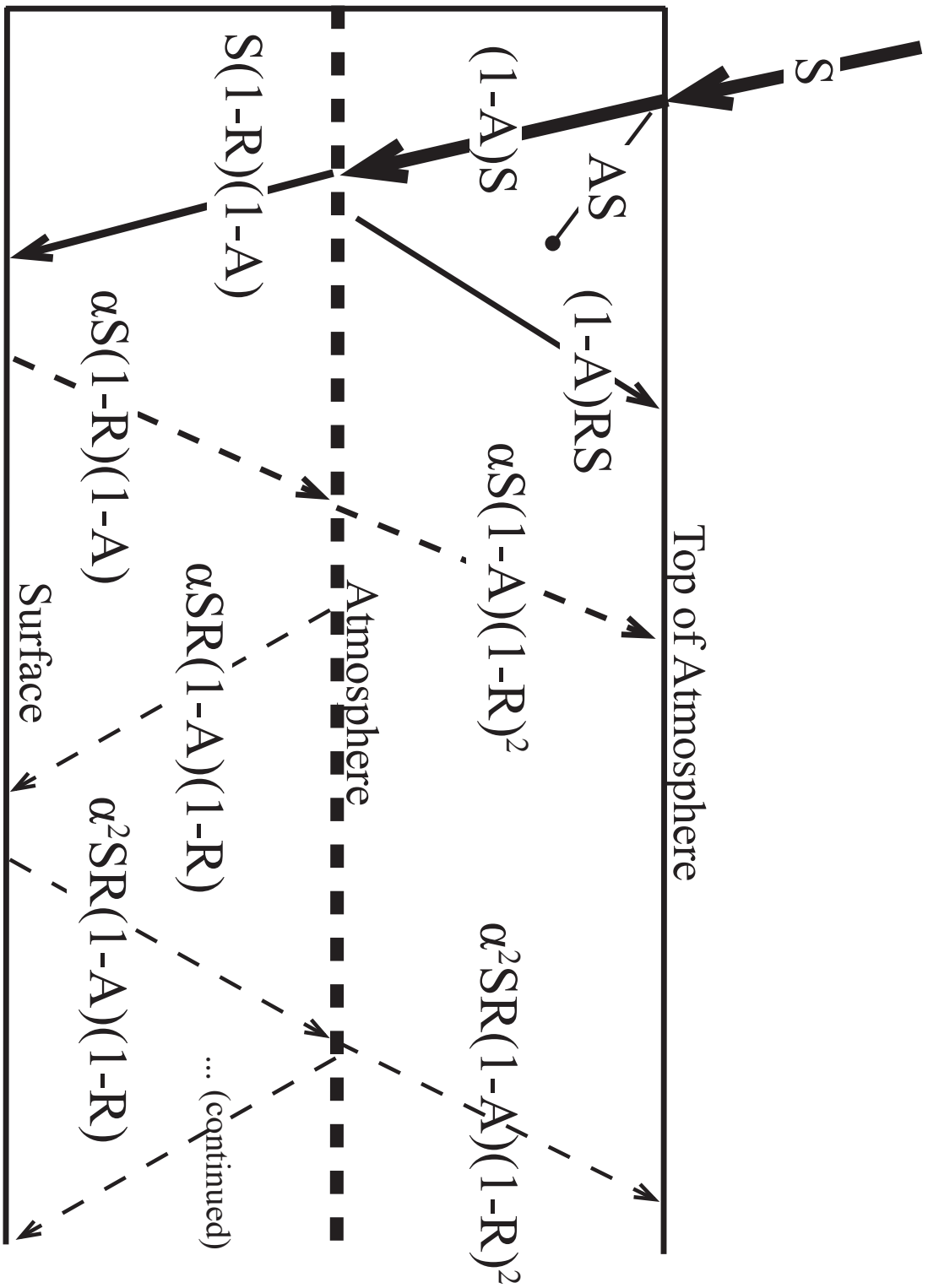


Figure 1: Schematic of the single layer isotropic model.

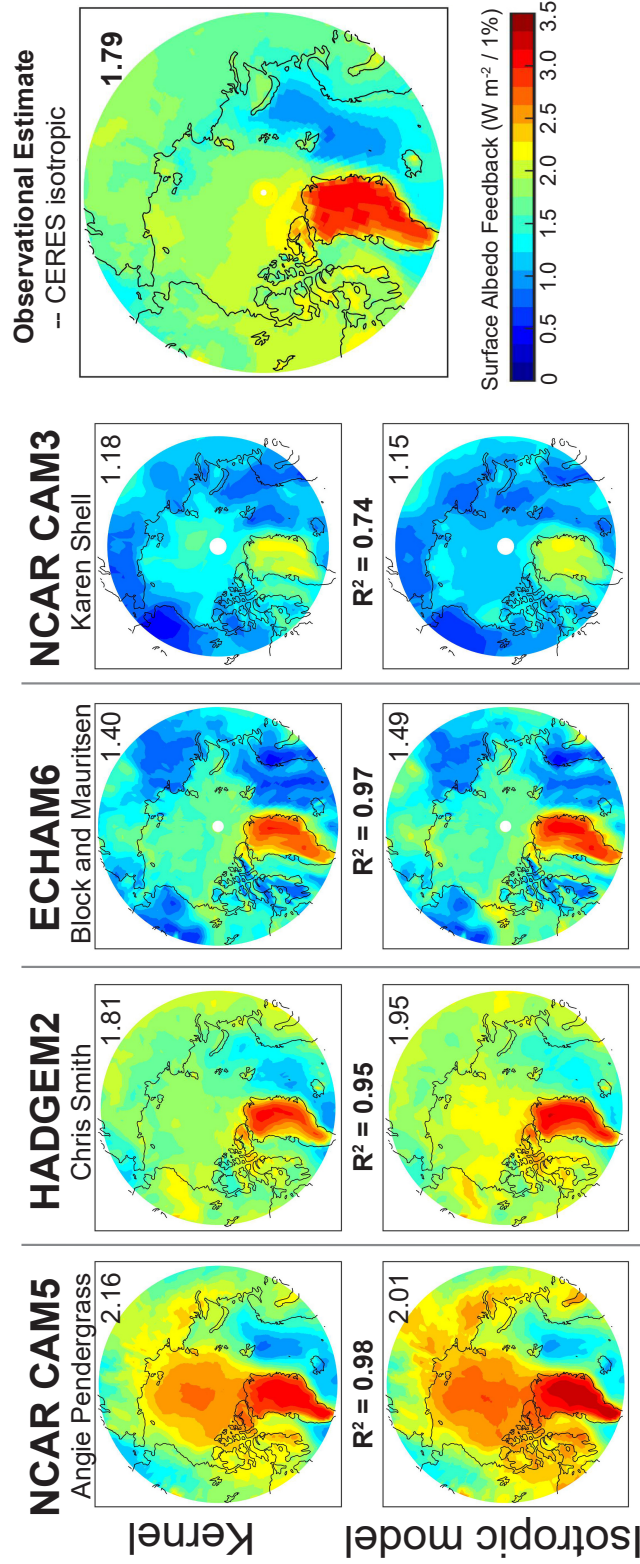


Figure 2: Arctic summertime (MJJA) surface albedo feedback calculated from radiative kernels (upper panels) and estimated from the climatological radiative fields using the idealized isotropic radiation model (lower panels) in the same models. The spatial correlation coefficient between the kernel isotropic methods in the same model are provided in the middle and the Arctic domain averaged values are shown in the upper right of each panel. Observational estimates from CERES EBAF satellite data and the isotropic model are shown to the right.

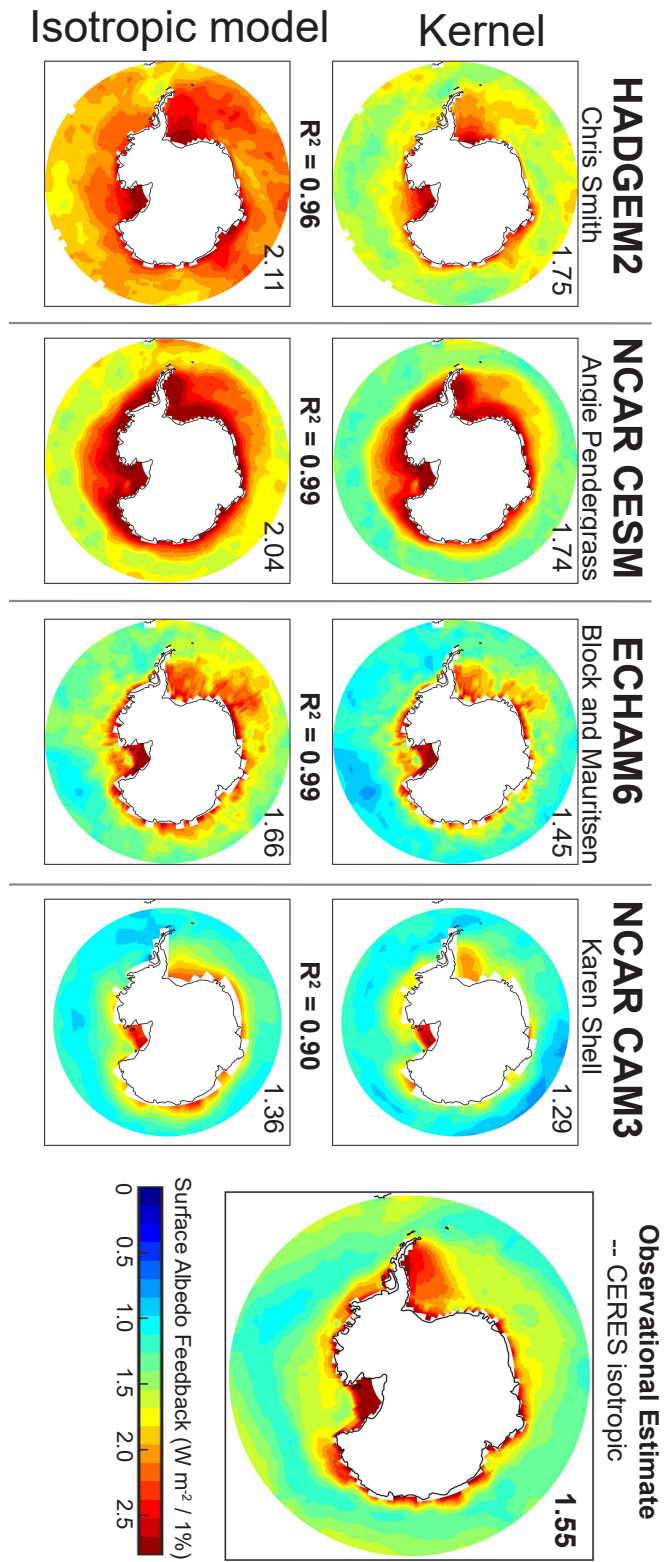


Figure 3: As in Fig. but for the Southern Ocean. Domain averaged surface albedo feedbacks exclude the Antarctic continent.

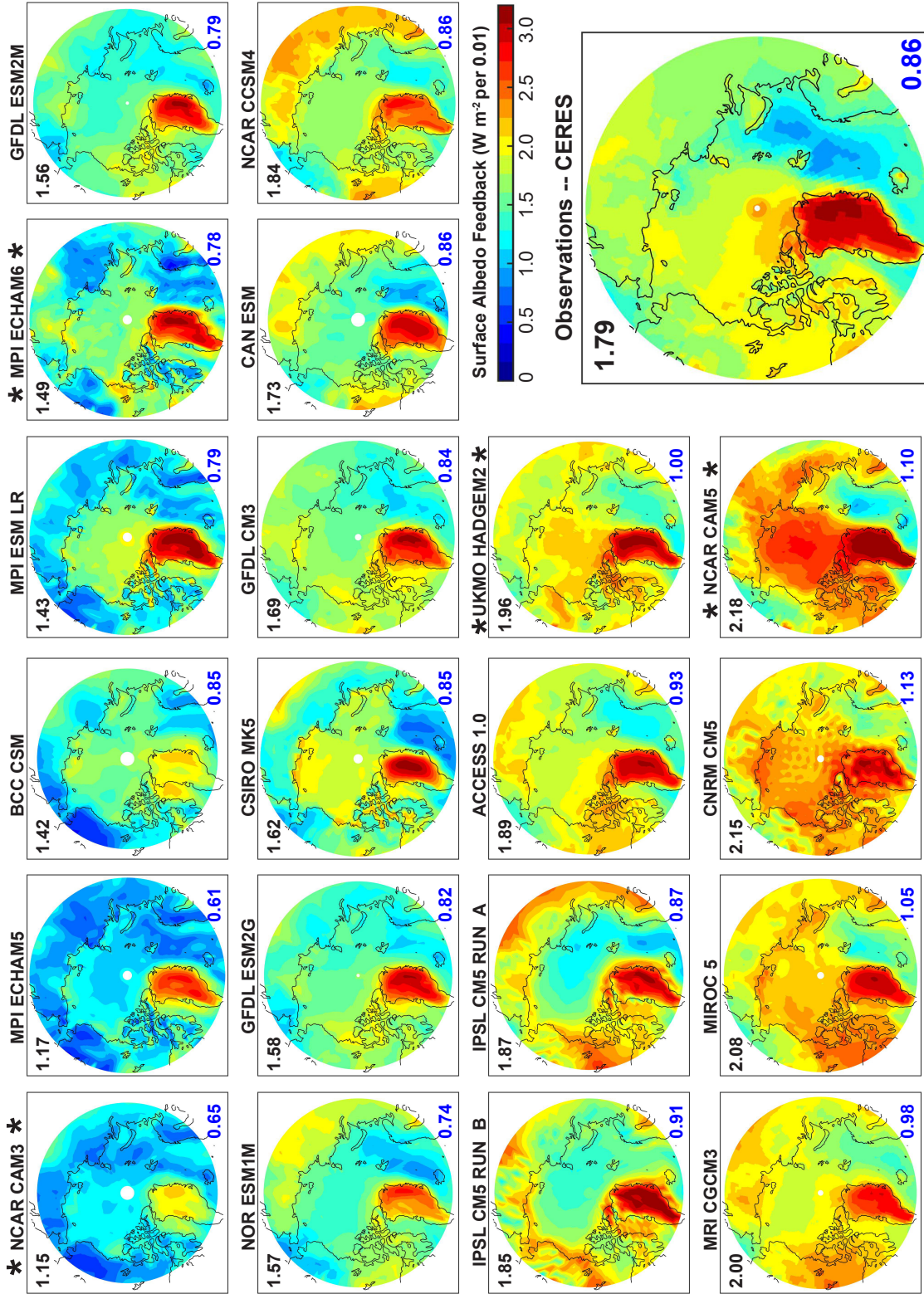


Figure 4: Arctic summertime (MJJA) surface albedo feedback estimated using the isotropic model and the climatological radiation fields for CMIP5 historical simulations. Models are ordered as in reading a book (left to right then down) according to the domain average albedo feedback. The full domain spatial average is shown in the upper left corner of each panel in black and the Arctic ocean average is shown in the lower right corner in blue. Observational estimates from CERES satellite data are shown in the bottom right panel.

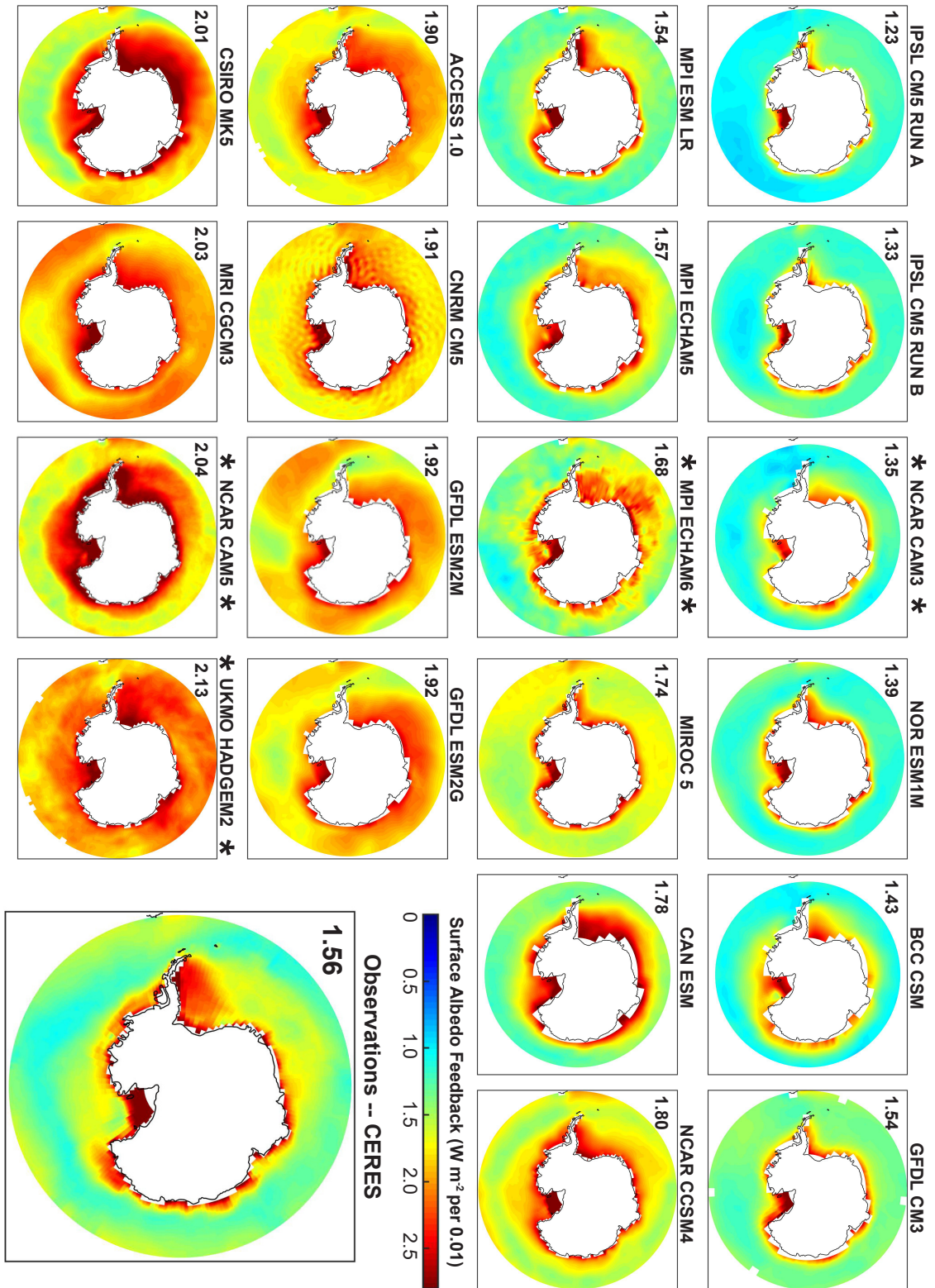


Figure 5: As in Fig. 3 but for the Southern Ocean. Domain averaged surface albedo feedbacks exclude the Antarctic continent.

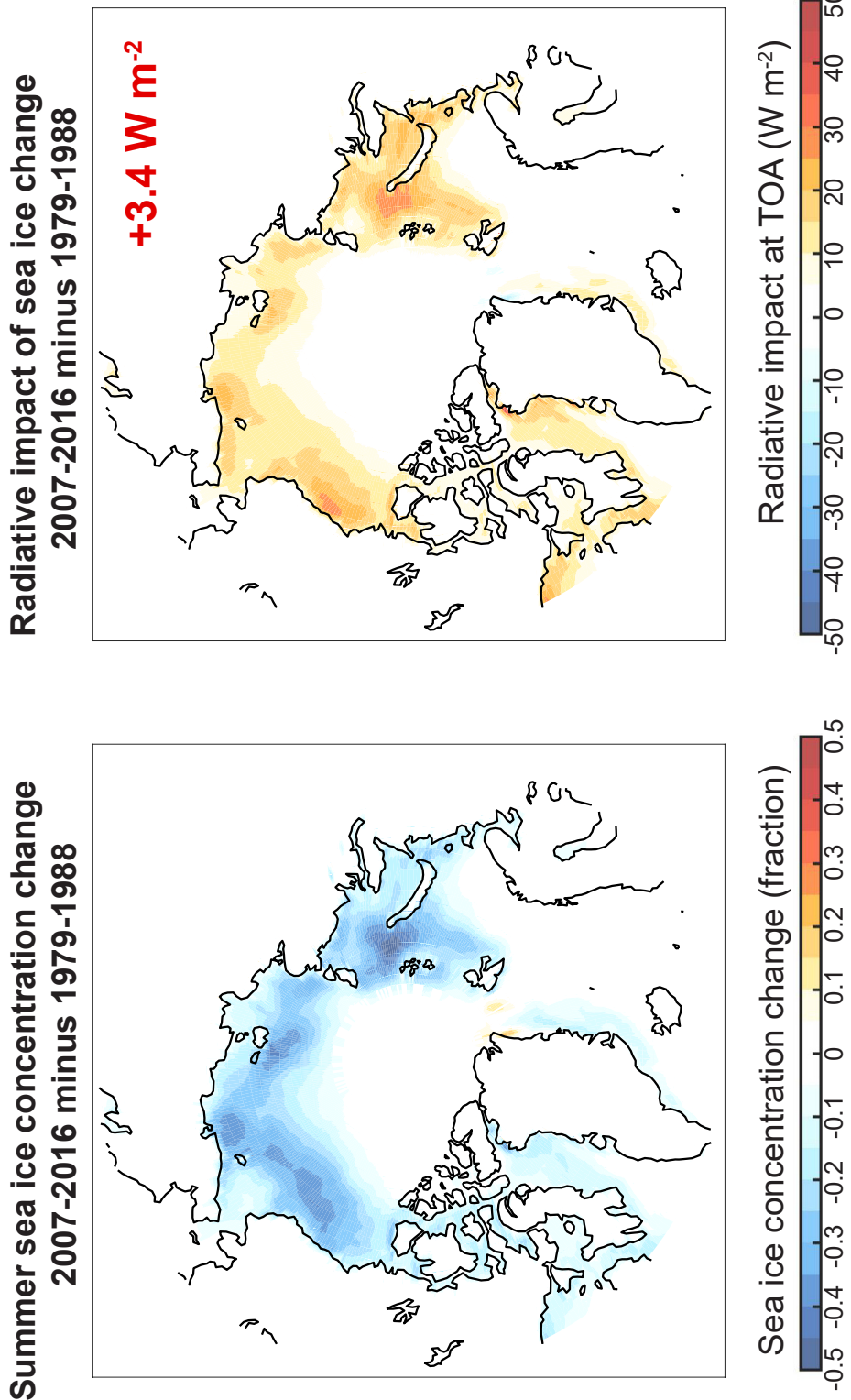


Figure 6: Observed sea ice concentration changes (left panel) and the associated change in radiation at the top of atmosphere (right) from the most recent decade (2007-2016) relative to the 1979-1988 average. Both calculations are the average values over the summer defined as May-June-July-August. The Arctic average radiative impact is shown by the red text in the right panel.

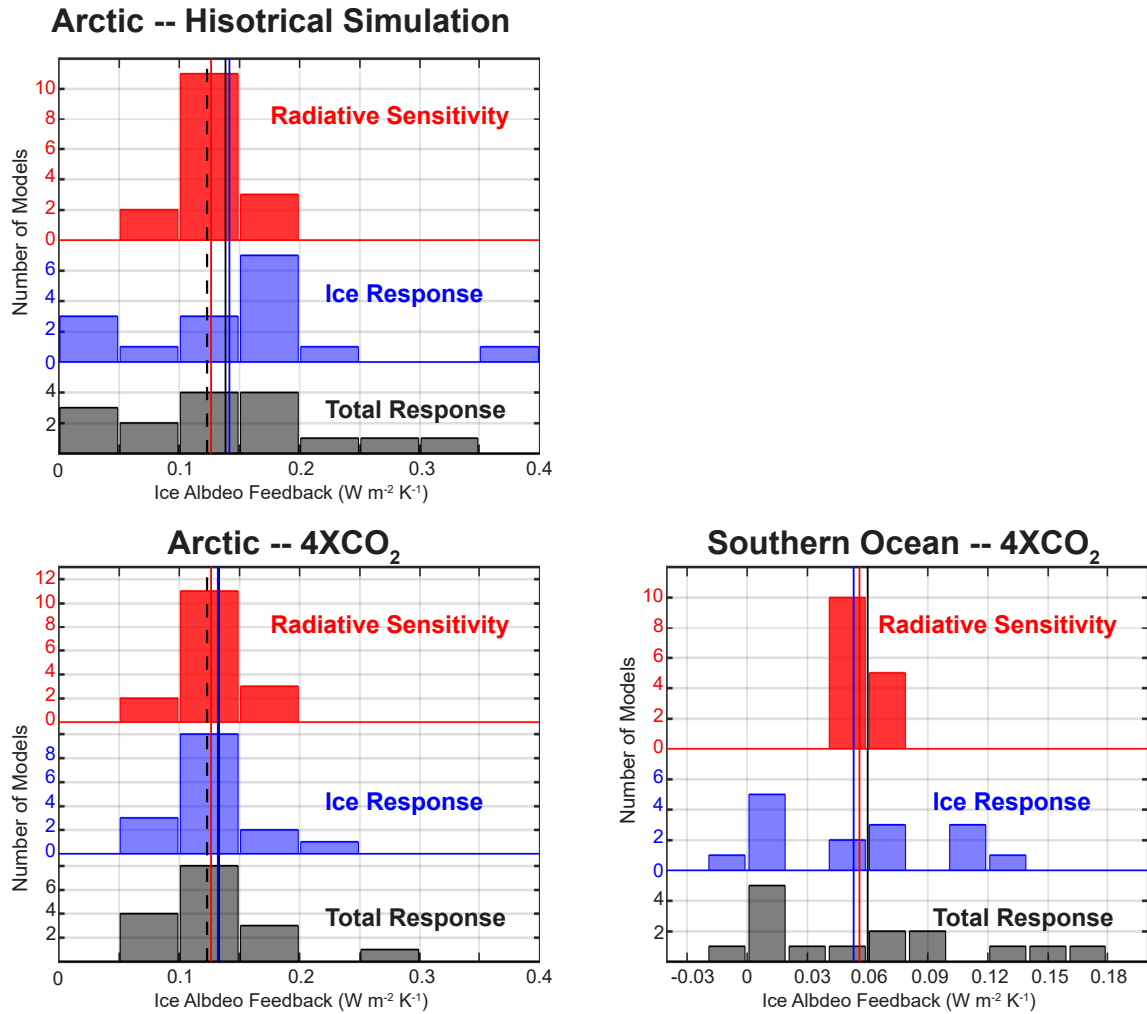


Figure 7: Estimates of surface albedo feedback spread from climate models and observations using the radiative sensitivity (RS) from the isotropic model applied to the climatology and and the change in surface albedo under external forcing normalized by the global mean temperature change. (Upper left) Sea ice changes over the historical (2007 to 2016 minus 1979 to 1988 averages). The black bars show the distribution using the model specific radiative sensitivity and ice changes, the blue bars show the distribution using the model specific sea ice changes and observational RS and the red shows the distribution using the observational sea ice change and model specific radiative sensitivity. Solid vertical lines show the model mean of each distribution and the black dashed line shows the observational estimate. (Lower Left) As in the above panel except using the modeled changes in the 4XCO₂ simulations. (Lower Right) Distribution of surface albedo feedback in the Southern Ocean diagnosed from 4XCO₂ normalized sea ice changes. Because the observational estimate of sea ice changes over the historical simulation is not statistically significant, the red distribution is calculated from the model specific radiative sensitivity and the model mean normalized sea ice change.